Using Thermochronology to Understand Orogenic Erosion

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Abstract

Erosion of orogenic mountain ranges exhumes deeply buried rocks and controls weathering, climate, and sediment production and transport at a variety of scales. Erosion also affects the topographic form and kinematics of orogens, and it may provide dynamic feedbacks between climate and tectonics by spatially focused erosion and rock uplift. Thermochronology measures the timing and rates at which rocks approach the surface and cool as a result of exhumation. Relatively well-understood noble gas and fission-track thermochronometric systems have closure temperatures ranging from $\sim 60$ to $\sim 550$°C, making them sensitive to exhumation through crustal depths of about one to tens of kilometers. Thus, thermochronology can constrain erosion rates and their spatial-temporal variations on timescales of $\sim 10^5$–$10^7$ years, commensurate with orogenic growth and decay cycles and possible climate-tectonic feedback response times. Useful methods for estimating erosion rates include inverting ages for erosion rates using crustal thermal models, vertical transects, and detrital approaches. Spatial-temporal patterns of thermochronometrically determined erosion rates help constrain flow of material through orogenic wedges, orogenic growth and decay cycles, paleorelief, and relationships with structural, geomorphic, or climatic features.

Key Words

geochronology, exhumation, orogeny, geomorphology, tectonics
INTRODUCTION

Orogens (mountain ranges formed by tectonic processes) control the patterns and scales of a wide variety of phenomena, including weathering, erosion, climate, hydrology, sediment transport and deposition, biotic distributions, and natural resources and hazards. The configuration and architecture of orogens also provide clues to the dynamics of mantle convection and the movement of tectonic plates, and the exhumed rocks within them provide samples of the deep crust and upper mantle. Understanding the growth and decay of orogens thus provides a basic framework for understanding many other natural processes and their interactions.

Three interrelated processes are commonly used to describe the tectonic geomorphology of orogens: rock uplift, surface uplift, and erosion. As clarified by England & Molnar (1990), rock and surface uplift describe the vertical motion of rock or a portion of Earth's surface, respectively, relative to a datum, such as sea level, that is suitably fixed. Erosion is the surficial removal of mass at a point in the landscape by both mechanical and chemical processes. It follows, then, that the difference between rock uplift and surface uplift is erosion. For example, surface uplift, which contributes to mountainous topography, only occurs when erosion is slower than rock uplift. Erosion is one type of the broader process of denudation, which, following Ring et al. (1999a), is the removal of rock or soil by tectonic and/or surficial processes at a specified point at or under Earth's surface. The other types of denudation are tectonic: normal faulting and ductile thinning. Incidentally, it is important to note that crustal thickening by ductile or brittle strain (e.g., thrusting) causes burial, not denudation, although thickening can produce high topography, which may result in erosion. Another term that is frequently used in studying orogenic evolution is exhumation, which Ring et al. (1999a) defined as the unroofing history of a rock, as caused by tectonic and/or surficial processes. Thus, exhumation is the history of or path taken by a particular rock toward the surface, as a result of a denudational process.

Erosion plays a critical role in orogenic evolution in several ways. First, it often follows rock and surface uplift in space and time, providing an indirect constraint on the spatial and temporal patterns of uplift in a landscape, which may be otherwise difficult to observe directly. More generally, erosion is a dynamic link between tectonic uplift and many other processes, including chemical weathering and long-term climate change, and sediment production, routing, and deposition. Most immediately, however, erosion directly influences not only topographic decay, but also growth of an orogen, by modulating the pattern and rates of surface uplift. Because erosion is also related to climate (e.g., precipitation), it provides an important feedback between climate and tectonics. Thus, interpreting how climate affects orogeny requires understanding erosion.

Rates of erosion over short timescales (1–10 years) can be estimated by sediment loads carried by rivers, but this can be difficult to extrapolate to longer timescales, largely because of the influence of large, infrequent erosional events, such as landslides (Hovius et al. 1997, Kirchner et al. 2001, Burbank 2002). Cosmogenic nuclide measurements made on fluvial sediment or in-situ materials can provide erosion rate estimates over timescales of typically $10^3$–$10^4$ years, capturing rates closer to
those over longer terms, and integrating an effective erosion rate signal through several meters depth (Brown et al. 1995, Bierman & Steig 1996, Granger et al. 1996, Kirchner et al. 2001, Riebe et al. 2003). However, many important geologic processes and feedbacks operate on timescales commensurate with large-scale rock deformation, at roughly $10^8$--$10^9$ year scales, requiring understanding of the spatial-temporal patterns of erosion on longer timescales. Erosion rates in active and decaying mountain ranges are typically $0.05$--$10$ km Myr$^{-1}$, with total erosion reaching depths of about $5$--$30$ km. These depths are too great for cosmogenic approaches, and, in many cases, total erosion depths are too shallow to estimate using thermobarometric-geochronologic constraints. Many radioisotopic thermochronometers, however, are well suited to this task because they are sensitive to temperature changes between about $60$--$550$°C, corresponding to crustal depths of about $2$--$10$ km.

In this chapter, we review general aspects of the use of thermochronology for the study of orogenic erosion, beginning with the fundamental bases of thermochronometric systems commonly used for this purpose, with an emphasis on K/Ar (and $^{40}$Ar/$^{39}$Ar), (U-Th)/He, and fission-track methods. We then review some basic concepts of the thermal structure of the shallow crust and how it is influenced by erosion and topography, and how these factors can be accounted for in the interpretation of thermochronologic data. We then describe several important techniques used in both active and decaying orogens for interpreting the spatial and temporal patterns of erosion, and provide examples illustrating the insights these approaches provide.

**THERMOCHRONOLOGY**

The (U-Th)/He, fission-track (FT), and $^{40}$Ar/$^{39}$Ar dating methods are the three main thermochronologic methods in use today that allow constraints on thermal histories at temperatures below approximately $300$--$550$°C. All are based on the production, by nuclear decay, of an isotope or radiation damage and the thermally controlled retention of these decay products. Radioisotopic production decreases exponentially with time but is predictable and otherwise steady, which gives the thermochronometer the ability to keep time. The thermal sensitivity of these radioisotopic clocks means that they provide information about the cooling history of rock, rather than the crystallization ages of its minerals (although in some cases they do record crystallization ages as well). We refer to these ages as cooling ages in that they tell us the duration of time that the dated mineral has been cool enough to retain the decay product of interest.

We provide a brief summary here, as needed to understand the thermal behavior of these dating methods. Interested readers are referred to Farley (2002), Wagner & van den Haute (1992), McDougall & Harrison (1999), and Hodges (2003) for more detailed accounts.

We use several idealized model calculations to illustrate the thermal behavior of the thermochronometers. All of the examples below were calculated using three programs, CLOSURE, AGE2EDOT, and RESPTIME (Brandon 2005, as summarized in Ehlers et al. 2005), which are available by following the Supplemental Material link from the Annual Reviews home page at [http://www.annualreviews.org](http://www.annualreviews.org).
Interested readers will find these programs useful for exploring thermochronometers or conditions not considered here.

(U-Th)/He Method
The (U-Th)/He method (He dating) is based on the accumulation of $^4$He produced by the decay of the parent isotopes $^{238}$U, $^{235}$U, $^{232}$Th, and $^{147}$Sm. Radiogenic $^4$He diffuses out of the mineral at a rate determined by the temperature and the He diffusivity of the mineral. Thus, the concentrations of $^4$He and the parent isotopes can be used to calculate a He cooling age. Measurements are typically made using a two-stage analytical procedure involving degassing of the crystal by heating and gas-source mass spectrometry to measure $^4$He, followed by inductively-coupled plasma mass spectrometry on the same crystal to measure $^4$U and Th (and, in some cases, Sm). Grain ages typically have a relative standard error (RSE) of approximately 3% to 5%, as determined by replicate measurements.

Fission-Track Method
The fission-track (FT) method utilizes the damage produced by fission decay of $^{238}$U. Fission causes $^{238}$U to split into two atomic fragments, which produces ionization damage along their repulsive paths. Fresh FTs have a total length of $\sim 11 \mu$m in zircon and $\sim 16 \mu$m in apatite. The track is thought to be a region of high defect density, not because of collision by the fission fragments, but rather because of changes in charge along the flight paths of the fission fragments. This ionization damage causes widespread dislocation of atoms from their stable lattice positions along the fission track (Fleischer et al. 1975). This interpretation explains why tracks are only found in nonconductive minerals. Thermally activated diffusion allows the defects to migrate and the damage to anneal. Thus, temperatures must remain low for FTs to be retained on a geologic timescale. The defects are known to have a range of activation energies for annealing (Ketcham et al. 1999), which accounts for the more complex retention behavior of FTs relative to that for He and Ar retention, which are well described by simple diffusion of an inert noble gas.

FTs are measured using a high-power optical microscope. The mineral grains to be dated are mounted, polished, and then chemically etched. The tracks etch more rapidly and thus become visible for counting. The concentration of the parent isotope is determined by neutron irradiation in a nuclear reactor, which induces fission of $^{235}$U. The natural $^{235}$U/$^{238}$U ratio is fixed, so the concentration of one isotope can be used to estimate the other. A sheet of U-free mica is placed over the polished grains of the mount. Chemical etching of this mica monitor reveals the density of induced $^{235}$U fission events. The induced tracks are also present in the mounted minerals, but they are not revealed given that the chemical etching of the minerals is done before the irradiation. The mica monitor and the mount are assembled with registration marks, which allows the operator to measure, in individual mineral grains, the spontaneous tracks (produced by $^{238}$U fission decay over geologic time) and the induced tracks (produced by neutron irradiation). FT grain ages have a RSE of $\sim 12\%$ for zircon.
and ~50% for apatite [median values from large compilation of detrital grain ages in Brandon (1996)]. FT ages are usually based on an average of many grain ages. In this case, the RSE for the age is typically 5% to 10%.

40Ar/39Ar Method

The 40Ar/39Ar method (Ar dating) is based on decay of 40K to radiogenic 40Ar. Like He, Ar is a noble gas, and the retention of 40Ar is controlled by thermally activated diffusion (although in some cases partitioning between phases can play an important role; Kelley & Wartho 2000, Baxter 2003). Argon diffusion is slower than that of He, probably owing mainly to its larger atomic radius. As a result, Ar cooling ages tend to be older than He cooling ages. Ar ages are determined by gas source mass spectrometry using a method that allows simultaneous determination of the parent 40K, often in the same subcrystalline diffusion domain. This is accomplished by conversion of some fraction of 39K to 39Ar by neutron irradiation prior to degassing and analysis. The concentration of the parent 40K can then be calculated knowing the production rate of 39Ar during the neutron irradiation and the 40K/39K ratio, which is fixed for natural K. The ratio of 40Ar/39Ar is then used to calculate the Ar cooling age. The RSE for grain ages is sometimes less than 1%, but the average is ~5% (e.g., 40Ar/39Ar grain ages for detrital white micas from Brewer et al. 2005). A key advantage of conventional 40Ar/39Ar dating is that step-heating and sequential gas analysis of single samples often reveals age spectra that reveal diffusion kinetics specific to the sample. These can often be modeled as representing continuous time-temperature histories (e.g., Harrison et al. 2005). Alternatively, 40Ar/39Ar ages can be measured in subcrystalline microdomains with high spatial resolution by laser ablation methods, to determine thermal, growth, or deformational histories (e.g., Kelley et al. 1994, Kramar et al. 2001, Mulch et al. 2002).

THERMALLY ACTIVATED DIFFUSION
AND PARTIAL RETENTION

There has been much study, both in the lab and in natural systems, of the thermal sensitivity of He, FT, and Ar retention and how this sensitivity can be used to estimate cooling histories. The most common approach is to use laboratory stepwise heating experiments to calibrate relationships between decay-product retention as a function of temperature and time (e.g., Fechtig & Kalbitzer 1966, Naeser & Faul 1969, Zeitler et al. 1987). These results are complemented by dating of drill samples from boreholes, where the modern thermal profile can be directly measured (e.g., Gleadow & Duddy 1981, Green et al. 1989, House et al. 2002, Stockli & Farley 2004). Exhumation by normal faulting has produced some exposed sections of continental crust. These settings have also proven useful for understanding retention behavior of thermochronometers as a function of increasing depth and temperature (Reiners et al. 2000, Stockli et al. 2000, Stockli 2005).

Although in general there is a remarkable degree of agreement among these methods, some studies have also identified important complexities in the thermal
Partial retention zone (PRZ): temperature or depth range where the radioisotopic decay products (e.g., $^{40}$Ar, fission tracks, or $^4$He) are only partially retained owing to thermally activated diffusion or annealing

PAZ: partial annealing zone, defined as the zone in the crust where FTs are partially retained. This term is synonymous with the more general term PRZ.

Laboratory diffusion experiments have demonstrated that on laboratory timescales the diffusivities of He and Ar are well fit by

$$D = D_0 \exp \left[ -\frac{E_a - PV_a}{RT} \right],$$

where $D_0$ is the frequency factor ($m^2$ s$^{-1}$), $E_a$ is the activation energy (J mol$^{-1}$), $P$ is pressure (Pa), $V_a$ is the activation volume (m$^3$ mol$^{-1}$), $T$ is temperature (K), $R$ is the gas law constant (8.3145 J mol$^{-1}$ K$^{-1}$), and $D$ is the diffusivity ($m^2$ s$^{-1}$). The $PV_a$ term is commonly taken as zero because most thermochronometers are retentive only at shallow depths in the crust ($<\sim 10$ km), where pressures are similar to those of the laboratory diffusion studies. Lister & Baldwin (1996) noted that subduction zone settings may provide an important exception for higher-temperature thermochronometers. The low-temperature, high-pressure conditions in subduction zones can result in temperatures of $350^\circ$C at $35$ km and deeper. Muscovite is able to retain Ar on geologic timescales at these temperatures, so the contribution of the $PV_a$ term is significant. We return to this issue below.

Measured diffusion properties from Table 1 are used to estimate the PRZ for commonly used He and Ar thermochronometers. Partial retention is usually measured...
Figure 1
Loss-only partial retention zones (PRZs) for common He, FT, and Ar thermochronometers. The PRZ for each thermochronometer is defined by upper and lower boundaries, indicating 90% and 10% retention, respectively, after being held at a steady temperature for a specified amount of time. Estimates shown were determined using the CLOSURE program with parameters in Tables 1 and 3.
### Table 1 Closure parameters for Ar dating

<table>
<thead>
<tr>
<th>Method (references)</th>
<th>$E_a$ (kJ mol$^{-1}$)</th>
<th>$D_0$ (cm$^2$ s$^{-1}$)</th>
<th>$a^*_s$ ($\mu$m)</th>
<th>$\Omega^{**}$ (s$^{-1}$)</th>
<th>$T_c^{10}$ (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^{40}$Ar/$^{39}$Ar K-feldspar (orthoclase) (Foland 1994)</td>
<td>183</td>
<td>$9.80 \times 10^{-3}$</td>
<td>10</td>
<td>$5.99 \times 10^3$</td>
<td>223</td>
</tr>
<tr>
<td>$^{40}$Ar/$^{39}$Ar Fe-Mg biotite (Grove &amp; Harrison 1996)</td>
<td>197</td>
<td>$7.50 \times 10^{-2}$</td>
<td>750 (500)</td>
<td>733</td>
<td>348</td>
</tr>
<tr>
<td>$^{40}$Ar/$^{39}$Ar muscovite (Robbins 1972, Hames &amp; Bowring 1994)</td>
<td>180</td>
<td>$4.00 \times 10^{-4}$</td>
<td>750 (500)</td>
<td>3.91</td>
<td>380</td>
</tr>
<tr>
<td>$^{40}$Ar/$^{39}$Ar hornblende (Harrison 1981)</td>
<td>268</td>
<td>$6.00 \times 10^{-2}$</td>
<td>500</td>
<td>1320</td>
<td>553</td>
</tr>
</tbody>
</table>

*$a_s$ is the effective spherical radius for the diffusion domain. Shown here are typical values. Muscovite and biotite have cylindrical diffusion domains, with typical cylindrical radii shown in parentheses. For these cases, $a_s$ is approximated by multiplying the cylindrical radius by 1.5.

**$\Omega$ is equal to $55D_0a_s^{-2}$ for Ar thermochronometers.

***$T_c^{10}$ is the effective closure temperature for 10° C Myr$^{-1}$ cooling rate and specified $a_s$ value.

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by considering the percentage retention of initial $^4$He or $^{40}$Ar after being subjected to a stepwise heating event. The loss-only PRZ is defined here by the temperatures associated with 90% and 10% retention for a specified holding time with steady temperatures. The percentage retention corresponds approximately to a similar reduction in the initial age. Note, however, that the loss-only PRZ ignores the production of new $^4$He, $^{40}$Ar, or FTs. As such, the definition focuses on the ability of a thermochronometer to retain information about old cooling events.

Wolf et al. (1998) defined a different kind of PRZ that accounts for both loss and production. The limits of the loss-and-production PRZ are defined by the temperatures needed to maintain a He, FT, or Ar age equal to 90% or 10% of the hold time for a steady thermal event. The time-temperature conditions associated with 90% and 10% retention are determined using the loss-and-production equation in Wolf et al. (1998), with the initial age set to zero (i.e., setting $^4$He$^*/P = 0$ in their equation 5). This type of PRZ is useful for understanding the evolution of cooling ages in a borehole. The CLOSURE program calculates both types of PRZs.

The loss-only PRZs for He and Ar dating (Figure 1a,c) were calculated using the exact versions of the loss-only diffusion equations given in Fechtig & Kalbitzer (1966) and McDougall & Harrison (1999). The following equations provide approximate solutions,

$$ T_{PRZ90\%} = \left[ -\frac{R}{E_a + PV_a} \ln \left( \frac{\pi a^2}{3600D_0t} \right) \right]^{-1} $$

and (2a)

$$ T_{PRZ10\%} = \left[ -\frac{R}{E_a + PV_a} \ln \left( \frac{-a^2}{\pi^2D_0t} \ln \left( \frac{\pi^2}{60} \right) \right) \right]^{-1}, $$

(2b)

which match the exact solutions to ~5° C to 10° C. These equations are included here to help illustrate the relationship between the holding time, given as $t$ (s), and the partial retention temperatures, $T_{PRZ90\%}$ and $T_{PRZ10\%}$. The parameter $a_s$ (m) is the equivalent spherical radius for the diffusion domain size.

For He dating of apatite, titanite, and probably zircon, the size of the diffusion domain scales with the natural size of the dated grain (Reiners & Farley 1999, Farley 2000, Reiners et al. 2004). At least in the case of apatite, diffusion is nearly isotropic,
so it can be modeled using a spherical diffusion geometry. However, apatite and zircon commonly have prismatic shapes, so the grain dimensions need to be converted to an equivalent spherical radius for this calculation. Fechtig & Kalbitzer (1966) and Meesters & Dunai (2002) showed that

\[ a_s \approx \frac{3V}{A}, \quad (3a) \]

where \( V \) and \( A \) refer to the volume and surface area, respectively, of the dated mineral grain. In contrast, Ar diffusion from most K-feldspars exhibits kinetic properties consistent with a heterogeneous assortment of domains, all of which are smaller than the physical grain size. McDougall & Harrison (1999) estimate that the Ar diffusion domains in K-feldspar have effective radii ranging from 1 to 100 µm.

The domain sizes for Ar diffusion in biotite, muscovite, and hornblende appear to be equivalent to the physical size of the dated grain. [Note that this issue is not fully resolved for biotite, as summarized by McDougall & Harrison (1999).] Argon diffusion is isotropic for hornblende and K-feldspar, so diffusion is modeled using a spherical geometry and \( a_s \) is estimated using Equation 3. Biotite and muscovite are anisotropic, with the fast direction of diffusion parallel to the basal plane. Ideally, one should use equations based on a cylindrical diffusion geometry, but we have opted to approximate the solution by converting the cylindrical radius \( a_c \) of the mica grains into an equivalent spherical radius, where

\[ a_s = 1.5 a_c, \quad (3b) \]

and then using this radius with the spherical solution for the diffusion equations. This approximation works well for estimating \( T_{PRZ90\%} \) and effective closure temperatures (introduced below), but less so for \( T_{PRZ10\%} \).

Apatite, titanite, and zircon are the main minerals dated by the He method. Among all thermochronometers that are currently thought to be well calibrated and understood, the He apatite system has the lowest PRZ temperatures. In fact, our PRZ calculations predict that apatite will lose measurable amounts of He when held at average surface temperatures (\( \sim 10^\circ \)C) for longer than \( \sim 250 \) Myr (Figure 1a). Ar dating is usually applied to K-feldspar, biotite, muscovite, and hornblende. Argon in hornblende has the highest PRZ temperatures relative to the other thermochronometers (Figure 1c).

The width of the PRZ increases systematically for those thermochronometers with greater PRZ temperatures. For instance, the He PRZ spans a temperature range of 35°C, whereas the Ar hornblende PRZ has a temperature range of 100°C. This observation is important because cooling ages can become quite complicated if a sample remained for a long time in the PRZ (e.g., Reiners & Farley 2001, House et al. 2002). This possibility is more likely for Ar muscovite and Ar hornblende because of their larger PRZ.

The PRZs for both He and Ar dating are affected by the diffusion domain size, \( a_d \). The examples shown in Figure 1 are based on typical values for \( a_d \), but grain size may be quite different from typical. The grain size effect can be significant. For example, an increase in \( a_d \) for K-feldspar from 10 µm to 100 µm causes an increase in PRZ temperatures of \( \sim 40^\circ \)C. Pressure can also cause an increase in the PRZ temperatures.
especially for the higher temperature thermochronometers. For example, McDougall & Harrison (1999) estimate that \( V_a \) for biotite and muscovite is about 10 to 14 cm\(^3\) mol\(^{-1}\). An increase in pressure from 0 to 1 GPa (equal to a crustal depth of ~35 km) would cause an increase in the PRZ temperatures for these micas of ~40°C to 50°C. Composition can also influence the PRZ temperatures. For example, Ar retention in biotite appears to increase with increasing concentrations of Fe and F. For hornblende, Ar retention seems to increase with increasing Mg, Al, and Fe\(^{+3}/\text{Fe}^{+2}\). In contrast, the PRZ temperatures for He dating of apatite appear to be largely independent of composition.

The retention of FTs is also controlled by diffusion, but the process is more complicated than that for \(^4\text{He}\) and \(^{40}\text{Ar}\). FT retention is independent of grain size. Diffusion of fission-track defects probably occurs on multiple length scales, all of which are smaller than the length scale of an individual FT. As noted above, FT defects likely have a range of thermal stabilities, which means that FT annealing cannot be represented by a single diffusive process. Experimental studies have shown that the macroscopic activation energy increases with increasing annealing. Thus, the definition of the loss-only PRZ is best determined directly from stepwise-heating experiments. These data are used to define the isopleths for 90% and 10% retention as a function of time and temperature plot and then extrapolated to geologic timescales.

The retention isopleths are usually well approximated by the Arrhenius equation,

\[
t = \Omega^{-1} \exp \left[ -\frac{E_a}{RT} \right] \quad \text{or} \quad (4a)
\]

\[
\ln [t] = -\ln [\Omega] - \frac{E_a}{RT}. \quad (4b)
\]

where \( \Omega \) \((s^{-1})\) is a proportionality constant and \( t \) \((s)\) is the hold time. Equation 4b is used for FT retention data from stepwise heating experiments. The best-fit result is used to independently estimate Arrhenius parameters for the 90% and 10% retention isopleths (Table 2). The loss-only PRZ temperatures are given by

\[
T_{\text{PRZ,90\%}} = -\frac{E_a,90\%}{R \ln [\tau\Omega,90\%]} \quad \text{and} \quad (5a)
\]

\[
T_{\text{PRZ,10\%}} = -\frac{E_a,10\%}{R \ln [\tau\Omega,10\%]} . \quad (5b)
\]

One can see from Figure 1b that the PRZ temperatures for apatite FT and zircon FT are influenced by several factors. Green et al. (1985) were first to recognize that the FT retention in apatite increased with increasing Cl content. More recent studies suggest that OH, Fe, Mn, and the rare earth elements probably also contribute to increased FT retentivity in apatite (Carlson et al. 1999, Donelick et al. 1999, Ketcham et al. 1999, Barbarand et al. 2003). Recent experimental work by Wendt et al. (2002) suggests that FT retentivity in apatite might increase with increasing pressure. This result is surprising given the good agreement between laboratory and borehole studies for FT retention in apatite (Kohn et al. 2003). Furthermore, there is no pressure effect
Table 2  Closure parameters for He and FT dating

<table>
<thead>
<tr>
<th>Method (references)</th>
<th>$E_a$ (kJ mol$^{-1}$)</th>
<th>$D_0$ (cm$^2$ s$^{-1}$)</th>
<th>$a_i^*$ (μm)</th>
<th>$\Omega^*$ (s$^{-1}$)</th>
<th>$T_{c,10}^{***}$ (C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(U-Th)/He apatite (Farley 2000)</td>
<td>138</td>
<td>50</td>
<td>60</td>
<td>$7.64 \times 10^7$</td>
<td>67</td>
</tr>
<tr>
<td>(U-Th)/He zircon (Reiners et al. 2004)</td>
<td>169</td>
<td>0.46</td>
<td>60</td>
<td>$7.03 \times 10^5$</td>
<td>183</td>
</tr>
<tr>
<td>(U-Th)/He titanite (Reiners &amp; Farley 1999)</td>
<td>187</td>
<td>60</td>
<td>150</td>
<td>$1.47 \times 10^7$</td>
<td>200</td>
</tr>
<tr>
<td>FT apatite$^1$ (average composition$^2$) (Ketcham et al. 1999)</td>
<td>147</td>
<td>—</td>
<td>—</td>
<td>$2.05 \times 10^6$</td>
<td>116</td>
</tr>
<tr>
<td>FT Renfrew apatite$^2$ (low retentivity) (Ketcham et al. 1999)</td>
<td>138</td>
<td>—</td>
<td>—</td>
<td>$5.08 \times 10^5$</td>
<td>104</td>
</tr>
<tr>
<td>FT Tioga apatite$^3$ (high retentivity) (Ketcham et al. 1999)</td>
<td>187</td>
<td>—</td>
<td>—</td>
<td>$1.57 \times 10^8$</td>
<td>177</td>
</tr>
<tr>
<td>FT zircon$^4$ (natural, radiation damaged) (Brandon et al. 1998)</td>
<td>208</td>
<td>—</td>
<td>—</td>
<td>$1.00 \times 10^8$</td>
<td>232</td>
</tr>
<tr>
<td>FT zircon (no radiation damaged) (Rahn et al. 2004, fanning model)</td>
<td>321</td>
<td>—</td>
<td>—</td>
<td>$5.66 \times 10^{13}$</td>
<td>342</td>
</tr>
<tr>
<td>FT zircon (Tagami et al. 1998, fanning model)</td>
<td>324</td>
<td>—</td>
<td>—</td>
<td>$1.64 \times 10^{14}$</td>
<td>338</td>
</tr>
</tbody>
</table>

$^*$ is the effective spherical radius for the diffusion domain. Shown here are typical values.

$^\Omega$ for FT thermochronometers is measured directly from experimental heating experiments and is equal to $55D_0a^2$ for He and Ar thermochronometers.

$^{***}T_{c,10}$ is the effective closure temperature for 10 °C Myr$^{-1}$ cooling rate and the specified $a_i$ value.

$^1$Recommended values for most geologic applications.

$^2$Average composition was taken from table 4 in Carlson et al. (1999). Equation 6 in Carlson et al. (1999) was used to estimate $r_{nv0} = 0.810$ for this composition. Closure parameters were then estimated using the HeFTy program (Ketcham 2005).

$^3$Closure parameters were estimated from HeFTy and $r_{nv0} = 0.8464$ and 0.1398 for Renfrew and Tioga apatites, respectively, as reported in Ketcham et al. (1999).

observed for FT retention in zircon (discussed below). More experiments are needed before this new result can be adequately assessed.

There has been much interest in finding an easily measured retention index or kinetic factor so that one could scale the retention behavior of FTs. Almost all of this work has focused on FTs in apatite. The $D_{par}$ and $r_{nv0}$ parameters of Ketcham et al. (1999) and Donelick et al. (1999) represent important steps toward this objective, but neither is able to provide confident predictions of FT retentivity over the full range of apatite compositions. Further progress on this problem would be aided by a better understanding of the atomic-scale processes associated with FT annealing. Carlson (1990) proposed the first mechanistic model for FT annealing, but Ketcham et al. (1999) have demonstrated significant deficiencies with the Carlson model.

We use the average apatite from Carlson et al. (1999) to define a reference for the FT retention of a typical apatite, as one might find in a sample of detrital apatites from sandstone. Their equation 6 was used to estimate the retention parameter $r_{nv0}$ for this average apatite composition and that parameter was then used with the HeFTy program (Ketcham 2005) to estimate the parameters in Table 3 for the loss-only PRZ. We used this same approach for the Renfrew and Tioga apatites, which Carlson et al. (1999) considered to be the least and most retentive, respectively, of the common naturally occurring apatites in their study. The average apatite has F:Cl:OH = 77:3:20 (numbers indicate the percent of cation substitution in the F site), and is thus mainly a fluorapatite, with some OH substitution. The Renfrew apatite is a
### Table 3  Parameters for FT partial retention zones

<table>
<thead>
<tr>
<th>Method (references)</th>
<th>Retention level</th>
<th>$E_a$ (kJ mol$^{-1}$)</th>
<th>$\Omega^1$ (s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>FT apatite$^2$ (average composition$^3$)</td>
<td>90%</td>
<td>127</td>
<td>$2.67 \times 10^5$</td>
</tr>
<tr>
<td></td>
<td>10%</td>
<td>161</td>
<td>$1.53 \times 10^7$</td>
</tr>
<tr>
<td>FT Renfrew apatite$^3$ (low retentivity)</td>
<td>90%</td>
<td>124</td>
<td>$1.91 \times 10^5$</td>
</tr>
<tr>
<td></td>
<td>10%</td>
<td>150</td>
<td>$4.39 \times 10^6$</td>
</tr>
<tr>
<td>FT Tioga apatite$^3$ (high retentivity)</td>
<td>90%</td>
<td>140</td>
<td>$1.41 \times 10^6$</td>
</tr>
<tr>
<td></td>
<td>10%</td>
<td>232</td>
<td>$3.38 \times 10^{10}$</td>
</tr>
<tr>
<td>FT Durango apatite</td>
<td>90%</td>
<td>160</td>
<td>$1.02 \times 10^{12}$</td>
</tr>
<tr>
<td></td>
<td>10%</td>
<td>195</td>
<td>$2.07 \times 10^{12}$</td>
</tr>
<tr>
<td>FT zircon$^2$ (natural, radiation damaged)</td>
<td>90%</td>
<td>225</td>
<td>$2.62 \times 10^{11}$</td>
</tr>
<tr>
<td></td>
<td>10%</td>
<td>221</td>
<td>$1.24 \times 10^{10}$</td>
</tr>
<tr>
<td>FT zircon (no radiation damage)</td>
<td>90%</td>
<td>272</td>
<td>$5.66 \times 10^{13}$</td>
</tr>
<tr>
<td></td>
<td>10%</td>
<td>339</td>
<td>$5.66 \times 10^{13}$</td>
</tr>
<tr>
<td>FT zircon (fanning model)</td>
<td>90%</td>
<td>231</td>
<td>$1.09 \times 10^{12}$</td>
</tr>
<tr>
<td></td>
<td>10%</td>
<td>359</td>
<td>$1.02 \times 10^{15}$</td>
</tr>
</tbody>
</table>

1 $E_a$ for FT thermochronometers is measured directly from experimental heating experiments.

2 Recommended values for most geologic applications.

3 Average composition was taken from Table 4 in Carlson et al. (1999). Equation 6 in Carlson et al. (1999) was used to estimate $r_{mr0} = 0.810$ for this composition. PRZ parameters were then estimated using the HeFTy program (Ketcham 2005).

4 PRZ parameters were estimated from HeFTy and $r_{mr0} = 0.8464$ and 0.1398 for Renfrew and Tioga apatites, respectively, as reported in Ketcham et al. (1999).

Table 3: Parameters for FT partial retention zones. The table lists various methods and their corresponding parameters for FT thermochronology, including retention levels, activation energies ($E_a$), and rate constants ($\Omega$). The data includes apatite and zircon samples, with some values reflecting average or mixed compositions. The table highlights the variability in retention properties and the importance of considering such parameters in geological analysis.

Nearly end-member fluorapatite, with F:Cl:OH = 97.5:0.5:2. The Tioga apatite is a mixed fluor/hydroxylapatite, with F:Cl:OH = 44:8:46 and 0.6% substitution of Fe$^{+2}$ into the Ca cation site. Figure 1b shows that the average apatite and the Renfrew apatite have similar PRZs. The Tioga apatite is much more retentive than the average apatite, with $T_{PRZ10\%}$ about 100°C greater.

This comparison indicates why variable FT retentivity in apatite is generally not a major problem. Fluorapatites have the lowest FT retentivity among all apatites, and most naturally occurring apatites have compositions close to that of an end-member fluorapatite. In contrast, increased retentivity can occur by several types of substitution, with Cl and OH substitution being the most important. Care is needed to screen for highly retentive apatites, a task that is especially important when dating detrital apatites from sedimentary rocks.

Zircon also shows a range in FT retention (Figure 1b). The main factor appears to be radiation damage by alpha decay (Nasdala et al. 2001, Ewing et al. 2003), which causes a decrease in FT retentivity (Kasuya & Naeser 1988). Compositional effects have not been recognized. Several experimental studies have shown that pressure has no significant influence on retentivity (Fleischer et al. 1965, Brix et al. 2002, Yamada et al. 2003). Rahn et al. (2004) estimated a no-damage PRZ using a compilation of published annealing experiments done on damage-free zircons. The natural radiation...
damage in these zircons was removed by heating, and then neutron irradiation was used to induce new FTs. Brandon et al. (1998) estimated a PRZ for natural radiation-damaged zircon using 1-h annealing experiments from Tagami et al. (1990), and a downhole suite of ZFT ages from a deep borehole in Germany (Zaun & Wagner 1985). They also compared the estimated PRZ with other field-based constraints, including estimates of closure temperature from other thermochronometers (discussed below). The zero-damage zircons indicate a \( T_{PRZ,10\%} \) that is \( \sim 125^\circ\)C greater than that estimated for natural radiation-damaged zircon. The PRZ labeled by Tagami et al. was estimated from a comprehensive laboratory study of FT annealing in natural zircon from a 21-Ma dacite tuff (Yamada et al. 1995, Tagami et al. 1998). Notably, the 10% retention isopleth for this study of radiation-damaged zircon is identical to that for the zero-damage zircon reported by Rahn et al. (2004) (Figure 1b). In laboratory heating experiments, alpha radiation damage appears to anneal at lower temperatures than FTs (Tagami et al. 1998). Garver & Kamp (2002) have shown that, at geologic timescales, alpha radiation damage, at least as indicated by zircon color, is retained at temperatures above the FT PRZ. When calibrating thermochronometers, there is no automatic assurance that diffusion and annealing studies conducted at laboratory timescales will be applicable at geologic timescales. We conclude for zircon FTs that retentivity changes with time owing to changes in the thermal stability of alpha damage. At geologic timescales, alpha damage is able to persist to high temperatures where it reduces the retentivity of associated FTs. Rahn et al. (2004) argued that the naturally calibrated PRZ is probably appropriate for most geologic settings. However, the zero-damage PRZ would be more appropriate for settings where the rocks have rapidly cooled from high initial temperatures (\( > 350 \) to \( 400^\circ\)C). In this case, there would be no time to form alpha damage. High-temperature metamorphic core complexes might be a typical example.

**EFFECTIVE CLOSURE TEMPERATURE**

Dodson (1973, 1979) published an analytical solution for the evolution of a thermochronometer that cools at a steady rate and whose retention behavior is controlled by thermally activated diffusion. His solution provides an estimate of the effective closure temperature, \( T_c \), defined as the temperature of the dated mineral at the time indicated by the thermochronometer. We know that a thermochronometer closes over a temperature range (as suggested by our PRZ estimates), but the measured cooling age will, by definition, point to just a single temperature on the cooling path.

We emphasize that \( T_c \) is only defined for the case of steady cooling through the PRZ, but this assumption is reasonable for eroding mountain belts, given the narrow temperature range for the PRZ and the slow response of the thermal field to external changes. In contrast, this assumption will likely fail and \( T_c \) will have little meaning in cases involving reheating by local igneous intrusions, hydrothermal circulation, or depositional burial.
Dodson (1973, 1979) estimated \( T_c \), using

\[
T_c = \frac{\Omega RT_c^2}{E_a + PV_a} \exp \left[ -\frac{E_a - PV_a}{RT_c} \right],
\]

(7)

where \( \dot{T} \) is the cooling rate, and \( \Omega \) and \( E_a \) are closure parameters, as defined in Tables 1 and 2. The \( PV_a \) is included for completeness, but the influence of pressure is generally taken to be negligible, as noted before.

For He and Ar dating, \( \frac{\Omega}{\epsilon_0} = 55 \) as, where \( as \) is the equivalent spherical radius for the diffusion domain. \( E_a \) and \( D_0 \) are given in Tables 1 and 2, along with typical values for \( a_s \). The relationships discussed with Equations 3a and 3b above can be used to make specific estimates for \( a_s \).

Dodson (1979) outlines the use of Equation 7 for estimating \( T_c \) for FT dating. He recognized that FT annealing does not follow a first-order rate law (Green et al. 1988). He argued that the 50% retention isopleth should provide reasonable estimates for \( E_a \) and \( \Omega \) in Equation 7. This approach makes sense given that the steady monotonic cooling path used for the closure temperature solution must pass through the full PRZ and thus would sample the full range of variation in the retention isopleths. The estimation of these parameters is the same as shown for Equation 5, but in this case, the fitting is done using the 50% retention isopleth. \( T_c \) can be estimated directly using a track-modeling program, such as HeFTy (Ketcham et al. 1999, Ketcham 2005). We have found that the \( T_c \) estimated by track-modeling programs is nearly identical (±1 °C) to that given by the Dodson equation.

Kohn et al. (2003) claimed that the effective closure temperature concept does not apply to FT dating. FT dating is commonly used to determine thermal histories for sedimentary basins, where the time-temperature path can include both heating and cooling within the PRZ. We agree that the closure temperature concept does not apply in this case, but this point holds for any thermochronometer where cooling through the PRZ is not steady and monotonic. Other methods, such as the HeFTy program, are needed to interpret the thermal histories. Nonetheless, we find that \( T_c \) is useful for thermochronologic studies of erosion and exhumation in mountain belts where steady monotonic cooling through the PRZ tends to be the rule, rather than the exception.

Figure 2a shows \( T_c \) as a function of cooling rate for the He, FT, and Ar thermochronometers, using the parameters from Tables 1 and 2. The cooling rate has an important effect on the relationship between cooling age and erosion rate, as discussed below. The general rule is that \( T_c \) increases with increasing cooling rate. Furthermore, the cooling rate effect becomes more pronounced with increasing retentivity of the thermochronometer. For instance, \( T_c \) for the apatite He system increases ∼13 °C per tenfold increase in cooling rate, whereas \( T_c \) for the hornblende Ar system increases ∼43 °C for the same cooling rate increase.

We note that for some minerals, in certain circumstances crystallization temperatures could potentially be similar to or even lower than the nominal \( T_c \). For example, white mica and K-feldspar can crystallize at temperatures well below their respective \( T_c \) values. In this case, the age of the thermochronometer would record the time of crystallization. Although some thermal history constraints may still be possible in
such cases, the closure temperature concept does not strictly apply, and this could potentially confound attempts to relate thermal and exhumational histories. This underscores the need to consider the conditions of a mineral’s formation, as well as its cooling path, in interpreting thermochronologic histories.

**Figure 2b** provides a comparison of the various $T_c$ estimates for apatite and zircon FT dating. $T_c$ for the average apatite is only $\sim 10^\circ$C higher than that for an end-member fluorapatite, as represented by the Renfrew apatite. In contrast, the $T_c$ for the Tioga apatite is $\sim 60^\circ$C above that for the average apatite. This range in $T_c$ would give a 7 Myr spread of FT ages for a typical orogenic cooling rate of $\sim 10^\circ$C Myr$^{-1}$. FT dating of detrital apatites in thermally reset sandstones commonly yields over-dispersed grain ages, which means that the range of grain ages is much greater than expected owing to analytical errors alone. This result is probably a consequence of a mix of apatite compositions, which gives a mix of retention behaviors. The $T_c$ estimates shown here indicate that the youngest grains in a grain age distribution should be dominated by low-retentivity apatites. Peak-fitting methods can be used to isolate the minimum age, which is the age of the youngest fraction of grain ages (Galbraith & Green 1990; Galbraith & Laslett 1993; Brandon 2005, as summarized...
in Ehlers et al. 2005). This approach provides a reliable way to isolate the FT age of the less retentive apatites in a reset grain-age distribution (Brandon et al. 1998, Zattin et al. 2002).

**Figure 2b** also illustrates the range of $T_c$ estimates for the zircon FT system. We have already noted that the FT retention in zircon appears to be strongly influenced by radiation damage. The $T_c$ estimates for zircon FT annealing experiments of Tagami et al. (1998) are nearly identical to those for the zero-damage zircons of Rahn et al. (2004). Annealing in natural radiation-damaged zircons indicates $T_c$ values that are lower by $\sim 110^\circ$C (Brandon et al. 1998). There are at least three studies that have used cross-calibration between different thermochronometers to make field-based estimates of $T_c$ for the zircon FT system (Harrison et al. 1979, Hurford 1986, Foster et al. 1996). All agree closely with predictions based on natural radiation-damaged zircon (see compilation in Brandon et al. 1998). The $T_c$ for zero-damage zircons may be applicable to settings where the zircons cooled rapidly from high initial temperatures ($>350$ to $400^\circ$C), given that there would be little alpha damage in these zircons during closure.

**EROSION, TEMPERATURE, AND COOLING AGE**

Our objective here is to illustrate the relationship between erosion rates and cooling ages. As a first step, it is necessary to consider how the thermal profile in the crust is affected by erosion. Consider a one-dimensional steady-state thermal field in an infinite layer of thickness $L$. The base and top of the layer are held at constant temperatures of $T_L$ and $T_S$, respectively. Material moves through the layer at a constant velocity $w$. This situation simulates a steady-state orogen where accretion at the base of the orogen is balanced by surface erosion at the same rate, so that $w = \dot{\varepsilon}$, where $\dot{\varepsilon}$ is erosion rate. The thickness of the orogen remains steady and the vertical velocity through the orogen is approximately uniform and steady.

This upper surface of the model is equivalent to the mean elevation of the local topography in the study area. It is well known that isothermal surfaces will tend to follow the long-wavelength form of the topography (Braun, 2002). Those perturbations are centered, however, on the depth predicted by the one-dimensional solution here. Thus, one can think of this solution as providing a description of the mean depth of the isothermal surfaces, relative to the mean elevation of the overlying topography. (The influence of topography on thermal structure is discussed in more detail below.)

Batt & Brandon (2002) show that this one-dimensional, steady-state solution provides a good approximation even when the horizontal velocities in the orogen are significant. Incoming accreted material is assumed to maintain the base of the orogen at a fixed temperature, as represented by $T_L$ at a depth $L$. Most thermochronometers have closure isotherms that are shallower than $\sim 10$ to $15$ km. We have found that the thermal structure in the upper part of the one-dimensional solution is fairly insensitive to the thickness of the layer and to the nature of the basal boundary condition, as long as $L$ is at least two or three times the closure depth. Thus, the solution works well for the He and FT thermochronometers and less well for the Ar thermochronometers.
The Peclet number, $P_e = \frac{\dot{\varepsilon}}{\kappa}$, is used to choose between two one-dimensional thermal solutions, where $\kappa$ is the average thermal diffusivity of the layer. The first solution accounts for heat transport associated with erosion, which becomes significant when $P_e$ is significantly greater than zero,

$$T(z) = T_S + \left( T_L - T_S + \frac{H_T L}{\dot{\varepsilon}} \right) \left( 1 - \frac{\exp(-\dot{\varepsilon} z/\kappa)}{1 - \exp(-\dot{\varepsilon} L/\kappa)} \right) \frac{H_T z}{L},$$  \hspace{1cm} (8a)

where $z$ is depth. As $P_e$ approaches zero, the solution is given by

$$T(z) = T_S + \frac{(T_L - T_S)z}{L} + \frac{H_T z(L - z)}{2\kappa}.$$  \hspace{1cm} (8b)

The layer is assigned a uniform internal heat production $H_T$, which is specified in units of °C Myr$^{-1}$. The more common practice is to use an exponentially decreasing heat production, but this approach seems inappropriate for many convergent orogens where the crust is composed mainly of recently accreted rocks. Figure 3 shows the thermal profile as a function of different steady erosion rates.

Erosion causes temperatures to increase in the upper part of the crust. We use thermal parameters for the northern Apennines of Italy for the examples calculated here. The Apennines represents a fairly typical convergent orogen (Vai & Martini 2001). We estimate that $L = 30$ km, $\kappa = 27.4$ km$^2$ Myr$^{-1}$, and $T_S = 14$ °C. In areas without erosion, the surface thermal gradient is $\sim 20$ °C km$^{-1}$, which is equal to a “no-erosion” surface heat flux $Q_S = 40$ mW m$^{-2}$. Our estimates of the internal heat production and the temperature at the base of the layer were guided by pressure-temperature estimates of deeply exhumed metamorphic rocks exposed within the orogen and the observed “no-erosion” surface heat flux. Our estimate for uniform internal heat production $H_T$ is 4.5 °C Myr$^{-1}$, which is equal to a volumetric heat production of 0.33 μW m$^{-3}$.

TL is estimated to be $\sim 540$ °C.

Next, we consider the effect of erosion rate on the depth of the effective closure temperature. Equation 8 provides a full description of the temperature and thermal gradient as a function of depth. The cooling rate is given by $\dot{T}(z) = \dot{\varepsilon} \frac{\partial T}{\partial z}$. The Dodson equation (Equation 7) provides a second equation relating $T_c$ to $\dot{T}$. An iterative search is used to find the depth $z_c$, which satisfies both equations; $z_c$ corresponds to $T_c$ and thus marks the depth of effective closure. The predicted cooling age is given by $z_c \dot{\varepsilon}$. Note that this $z_c$ is referenced to the mean elevation $b_m$ of the local topography. Samples reaching the surface at elevations $b$ other than the mean elevation will have predicted ages equal to $\frac{z_c - b_m + b}{\dot{\varepsilon}}$ (Brandon et al. 1998, Reiners et al. 2003b).

The colored lines in Figure 3 show $z_c$ and $T_c$ for the He apatite, FT zircon, and Ar muscovite thermochronometers as a function of erosion rate. There are two competing effects that determine the depth of the closure isotherm. Faster erosion causes all isotherms to migrate closer to the surface, but the steeper thermal gradient causes faster cooling and a larger $T_c$. Thus, the closure depth becomes shallower with faster erosion, but this response is offset by the increase in $T_c$ caused by faster cooling.

The relationship between erosion rate and cooling age for samples at the mean local elevation ($b = b_m$) is shown in Figure 4. For slow erosion ($< \sim 1$ km Myr$^{-1}$),
Figure 3

Influence of erosion rate on the thermal profile and closure temperatures at steady state. The thermal profiles are steady-state solutions for a one-dimensional thermal field with a steady erosion rate. Temperature is held fixed at the top and bottom of a 30-km thick infinite layer. Erosion is represented by a steady velocity through the layer. The specific thermal parameters used for this model are based on the northern Apennines of Italy, which is a fairly typical convergent orogen. The color lines show the effective closure temperature for apatite He (AHe), zircon fission track (ZFT), and muscovite Ar (MuAr) as a function of increasing erosion rate. The results were determined from the AGE2EDOT program, using the following procedure: For a specified erosion rate, the program finds the associated steady-state thermal profile and the cooling rates for that profile. The Dodson Equation (Equation 7) is then used with the parameters from Tables 1 and 2 to find the temperature and depth of effective closure for the thermochronometer of interest. This is repeated for many closely spaced profiles to give the continuous closure temperature curves shown in the figure.

Erosion rate and cooling age change proportionally. For example, if we double the erosion rate from 0.1 to 0.2 km Myr$^{-1}$, He apatite cooling ages would decrease by half, from 20 to 10 Ma. This proportionality is expected when erosion rates are too slow to move the closure isotherm. Now consider doubling of the erosion rate from 1 to 2 km Myr$^{-1}$. The He apatite age decreases by more than half, from 2 to 0.7 Ma. In this case, the erosion rates are fast enough to significantly change the depth of the closure isotherm. In fact, note that the slopes of the curves are 1:1 in the log-log plot.
Figure 4
Relationship of cooling ages to erosion rates at exhumational steady state for common He, FT, and Ar thermochronometers. Results were determined using the AGE2EDOT program. The thermal field is represented by a one-dimensional steady-state thermal field, as shown in Figure 3. Closure parameters are from Tables 1 and 2. The thermal parameters are based on the northern Apennines.

where erosion rates are slow. This situation indicates that that heat transport is mainly occurring by conduction. The steeper slopes at higher erosion rates indicate that a significant fraction of the heat moving through the layer is being carried advectively by the velocity of the rock toward the surface. Moore & England (2001) provide a detailed analysis of the thermal part of this problem, but they did not include the effect of cooling rate on closure temperature.
TIME TO EXHUMATIONAL STEADY STATE

The steady-state condition used above may seem overly simplistic. In fact, we know that the thermal profile requires time to reach steady state, especially for the deeper parts of the profile. For thermochronologic interpretation, we are not interested in a full thermal steady state, but rather in an exhumational steady state (Willett & Brandon 2002). Exhumational steady state means that the products of exhumation have become steady with time. For example, Bernet et al. (2001) argued that the central part of the Swiss Alps has been shedding zircons with a steady FT age since ∼25 Ma. This implies that both the exhumation rate and the closure depth have remained steady with time. We can define exhumational steady state using the normalized velocity of the closure isotherm, which is defined by the vertical velocity of the isotherm divided by the erosion rate. A normalized velocity of zero means that the closure isotherm has reached a steady-state position, whereas a normalized velocity of one means that the isotherm is moving upward at the same rate as the rock. There would be no cooling for this case.

Figure 5 shows the evolution of closure isotherms for He, FT, and Ar thermochronometers as a function of a stepwise increase in erosion rates from zero to a steady rate of 1 km Myr$^{-1}$. The normalized velocity of the closure isotherm is shown on the vertical axis. The normalized velocity for He apatite and FT apatite systems drops to 10% within 2.5 and 4 Myr, respectively, whereas it takes 8 Myr for the Ar muscovite system to reach this state. Thus, we can expect that the lowest temperature thermochronometers will reach exhumational steady state within a short period of time. It is important to note that, in nature, erosion rates probably do not change in a stepwise fashion. Slower changes will allow the closure isotherm to more closely follow the steady state solution shown in Figure 3.

TEMPORAL CHANGES IN EROSION: VERTICAL TRANSECTS

Erosion rates can vary with time and, in some cases, this temporal variation is of prime interest. One approach to constraining changes in erosion rates is to measure cooling ages of systems with different closure temperatures in the same rock. Combining the FT and (U-Th)/He systems on zircon and apatite from the same rock, for example, would provide cooling ages through temperatures of roughly 240°C, 180°C, 110°C, and 65°C, assuming a cooling rate on the order of 10°C Myr$^{-1}$. Cooling rates between the ages of any system pair can simply be calculated by dividing the difference in the closure temperatures by the difference in cooling ages. A simplistic estimate of the average erosion rate, can then be made by dividing the cooling rate by an assumed geothermal gradient. The geothermal gradient represents a major assumption in this calculation. As described above, erosion causes upward migration of isotherms, increasing the geothermal gradient, especially at shallow depths. If erosion is known to have been steady for a sufficiently long time to establish a steady-state thermal field, this isothermal compression can be accounted for, to first order, by assuming variable geothermal gradient as a function of depth. But if a constant exhumation rate
Figure 5
Response of the closure isotherm to the sudden onset of rapid erosion from 0 to 1 km/Myr. Results were determined using the RESPTIME program. The curves show the normalized velocity of closure isotherms with time after the initiation of rapid erosion for the common He, FT, and Ar thermochronometers. The normalized velocity is defined as the vertical velocity of the closure isotherm divided by the erosion rate. A normalized velocity of one means that the closure isotherm is moving with the same velocity as the rock relative to the surface. A normalized velocity of zero means that the closure isotherm has reached its steady-state depth. The thermal calculation is the same as before, except for the introduction of a finite-difference algorithm, which is needed to calculate the time evolution of the thermal profile. The thermal parameters are based on the northern Apennines. Closure parameters are from Tables 1 and 2.

has not proceeded long enough to establish a steady-state thermal field, the evolving thermal field will add additional complexity. Moore & England (2001) showed that for some time after a stepwise increase in erosion rate, cooling ages give the appearance of gradually increasing erosion rates with time. This result is an artifact of the migration of the closure isotherm to a new steady state depth (Figure 5).

An alternative approach that avoids some of the complications associated with an assumed geothermal gradient would be to examine bedrock cooling ages as a function of depth in an orogen. Obviously, without drilling to depths of at least several hundred meters it is not possible to sample a truly vertical transect. But mountainous regions often provide an approximation of this sampling approach. In some settings, rapid tectonic denudation by normal faulting, combined by isostatically induced tilting, has
exposed deeply exhumed footwall blocks that can be interpreted as inclined crustal sections through depths as great as ~15 km. In some cases, fossil PRZs are observed at depths that are consistent with reasonable preexhumation geothermal gradients, and cooling ages at greater depths record the onset and rate of tectonic exhumation (Reiners et al. 2000, Stockli et al. 2000, Stockli 2005).

In orogens dominated by erosional denudation, however, topographic relief may be taken to approximate crustal depth, with a vertical transect approximated by bedrock cooling ages measured from samples over a large elevation difference and a relatively short horizontal distance. The vertical transect method will commonly yield a simple age-elevation relationship (AER) that can be interpreted as the vertical velocity of the rocks relative to the closure isotherm at the time of closure. Changes in the slope of the AER with elevation are typically interpreted to represent changes in erosion rate with time. This method was first proposed and used by Wagner & Reimer (1972) and Wagner et al. (1977). Fitzgerald et al. (1995) provide a good review of this method. The vertical transect approach is based on three important assumptions: (a) that the closure isotherm was flat at the time of closure; (b) at a given time, erosion rates were the same for samples composing the AER (spatially uniform erosion rate); and (c) the depth of the closure isotherm has remained constant, so that cooling of rocks can be accurately considered to represent their movement, relative to the surface, through a stationary isotherm.

**Figure 6** shows an example of FT and (U-Th)/He cooling ages from rocks of the Coast Plutonic Complex in southeastern Alaska. This transect, collected over a horizontal distance of about 7 km, up the side of Mt. Hefty, has ~1.8 km of vertical relief (Donelick 1986, Hickes 2001). FT and ZHe ages vary between 40 and 60 Ma and show a steep trend of elevation relative to age, whereas AHe ages show a more gentle trend. The overall slope of the AER for the AHe ages is 0.078 ± 0.004 km Myr⁻¹. If the assumptions above are met, then this estimate indicates the rate of erosion at the time the rocks moved through the AHe closure isotherm (16–38 Ma). Variations in the slope of the AER between any two points in the transect could be interpreted to represent variations in exhumation rates at those times, but in this case such variation is not distinguishable from random error.

The AHe data also provide indirect constraints on the average erosion rate for the time of closure of the cooling ages to present. The closure depth is determined relative to the local mean elevation of the landscape. We define \( \tau_m \) as the cooling age at the present local mean elevation. The mean amount of eroded section from \( \tau_m \) to present is equal to the \( z_c \) at the time that \( \tau_m \) closed. For our example, \( \tau_m \) for AHe is 20 Ma and the erosion rate at that time was 0.08 km Myr⁻¹ as indicated by the slope of the AER. The exhumational steady-state solution (Figure 4) predicts that at this erosion rate, \( T_c = 55^\circ C \) and \( z_c \) would be 2.0 km, with an average thermal gradient of \( (35^\circ C - 10^\circ C)/2 \) km = 12.5 \(^\circ\)C/km (assuming a surface temperature of 10^\circ C). The predicted average erosion rate is 2.0 km/20 Ma = 0.1 km Myr⁻¹ for the interval from 20 Ma to present. The AER profile for the AHe ages, which is representative of erosion rates for the interval 38 to 16 Ma, indicates a similar rate of 0.08 km Myr⁻¹. Thus, the assumption of steady erosion is supported by the data.
Figure 6

Concepts underlying, and examples of, a thermochronologic vertical transect. (a) Samples (filled circles) are collected over a range of elevation and a small horizontal distance, i.e., valley bottom to ridge top, over topography with amplitude $h_0$ and wavelength $\lambda$. Consider the case of a steady erosion rate $\dot{e}$ through a flat closure isotherm (solid red line) at a depth $z_c$ below the mean elevation $h_m$. Two samples exposed at different elevations $h_r$ and $h_v$ would have a difference in age of $(h_r - h_v)/\dot{e}$. (b) ZFT (red), ZHe (orange), AFT (light blue), and AHe (dark blue) ages for samples from a vertical transect with 1.8 km of relief, collected over $\sim$7 km horizontal distance, on Mt. Hefty, southeastern Alaska (data from Donelick 1986, Hickes 2001). Regression through the AHe data indicates an exhumation rate of $0.078 \pm 0.004$ km Myr$^{-1}$ between $\sim$38 and 16 Ma. (c) The average erosion rate after closure is equal to $z_c/\tau_m$, where $\tau_m$ is the cooling age at the mean elevation in the landscape, which gives 0.10 km Myr$^{-1}$ for 20 Ma to present (see text for details). (d) Stacked pseudovertical transect. AHe ages are plotted in the normal way, but the other cooling ages are offset upward from their true elevations by a height equal to the difference in $z_c$ for that thermochronometer relative to $z_c$ for the AHe system.

Some studies have compared the zero-age intercept of the observed AER trend to the predicted closure depth, based on modern heat flow data, to estimate erosion rates during the interval between cooling ages and present (Parrish 1983, Farley et al. 2001). This approach is essentially the same as the one above, because the estimate of $z_c$ represents the predicted depth where the relevant thermochronometer would
show zero ages. Our approach and that used by Parrish (1983) are both based on a one-dimensional steady-state thermal model (e.g., Equation 8). We both use the modern “no-erosion” surface heat flux with the assumption that this quantity has not changed since \( \tau_m \). For the example above, the extrapolated AER trend intersects the elevation axis at our estimate of \( z_c \) for AHe (Figure 6c), indicating that there is no significant difference in erosion rates over the intervals 38–16 Ma and 20 Ma to the present. If the zero-age intercept of the AER trend was at an elevation significantly above (below) the estimate closure depth, this would be evidence that erosion rates had increased (decreased) after the ages of the samples composing the AER. The difference between the erosion rate inferred from the AER and the more recent one would be the difference in predicted closure depth and observed extrapolated intercept, divided by the inferred time of erosion rate change. Alternatively, a mismatch in predicted closure depth and zero-age intercept might indicate that our assumption of a steady “no-erosion” surface heat flux is wrong.

We can extend the AER by adding cooling ages for higher-temperature thermochronometers. This approach involves construction of a stacked pseudo-vertical transect (Reiners et al. 2003b), as shown in Figure 6d. The AHe ages are plotted in the normal way, as a function of age and elevation. The cooling ages for the other thermochronometers are plotted with their elevations shifted upward by an amount equal to the difference in \( z_c \) for the thermochronometer relative to that for the AHe thermochronometer. We use the AGE2EDOT program to estimate closure depths of 2.2 km for AHe, 4.5 km for AFT, 7.7 km for ZHe, and 10.2 km for ZFT. These depths are predicted using the same thermal parameters as for the examples above (e.g., Figure 5) and a steady erosion rate of 0.1 to 0.3 km Myr\(^{-1}\). The \( z_c \) estimates are fairly insensitive to the assumed erosion rate given the slow erosion for this area. The stacked pseudovertical transect for the ZFT, ZHe, AFT, and AHe systems (Figure 6d) shows that prior to 40 Ma, erosion was much faster, at a rate of \( \sim 0.5 \) km/Myr.

Interpretations of exhumation rates and their changes through time by these approaches can provide insights to the long-term evolution of orogens with sufficient topographic relief, but they are limited by the assumptions described above. One of the most important of these assumptions is that the closure isotherm is flat and not bent by topography (Figure 6a). Closure isotherms are likely to have significant topography where the closure temperature is low, the exhumation rate is high, or the topography over which samples are collected has a long effective wavelength. As shown by numerous studies, violation of the flat closure isotherm assumption (in the case of no relief change) has the general effect of rotating the AER to a steeper trend, resulting in a high-side bias for the erosion rates measured from the AER (Stuwe et al. 1994, Mancktelow & Grasemann 1997, Braun 2002, Reiners et al. 2003b). For the AHe and AFT systems, topography with wavelengths greater than about 10 km and 18 km, respectively, has the effect of bending closure isotherms by more than about 20%, which will cause a similar (~20%) upward bias in the exhumation rate estimated directly from an AER. The sensitivity of closure isotherms of these systems to topography has also been used to an advantage, however, by studies examining paleotopography (House et al. 1998) and its evolution over time (Braun 2002).
Detrital Thermochronology

Another approach to understanding orogenic denudational histories uses cooling ages of detrital minerals eroded from exhumed bedrock and preserved in sediment or sedimentary rocks (e.g., Cerveny et al. 1988, Copeland & Harrison 1990, Brandon & Vance 1992, White et al. 2002). Geochronology of detrital minerals has a long history, especially U/Pb dating of detrital zircons to constrain provenance and ages of sedimentary rocks whose sources are unknown. Beyond provenance, however, U/Pb crystallization ages are often of little use for understanding orogenic erosional histories. The vast majority of zircons eroded from the Himalayas, for example, have zircon U/Pb ages older than 500 Ma, reflecting ancient magmatic or metamorphic events unrelated to the Cenozoic Himalayan orogen. In contrast, most of the (U-Th)/He cooling ages on these same zircons are younger than 4 Ma (Campbell et al. 2005), reflecting cooling associated with rapid exhumation from ZHe closure depths. Thus, thermal history information from thermochronology of detrital minerals is necessary for understanding the erosional history of orogens. Approaches for obtaining both crystallization and cooling ages by combined single-grain U/Pb and (U-Th)/He ages in detrital zircons have recently offered new insights to provenance and exhumation histories in detrital studies (Rahl et al. 2003, Campbell et al. 2005, Reiners et al. 2005a).

Detrital thermochronology offers at least two advantages over bedrock approaches. One is that detrital cooling ages in sedimentary rocks often preserve a much longer record of exhumation than can be obtained from exposed bedrock within the orogen of interest. Bernet et al. (2001), for example, used FT ages of zircons in middle Miocene to Recent sediments to demonstrate exhumational steady state of the European Alps over this time interval. A second advantage is that rivers provide a convenient means of sampling over a large area, especially where access to bedrock exposures is difficult. A single well-mixed fluvial sediment sample may contain detrital contributions from nearly every part of a drainage. Provided analytical methods allow for sufficiently high sample-throughput, large numbers of individual grains can be analyzed to determine cooling age distributions representative of each drainage, which can be analyzed in several ways, as described below.

Lag Time

One goal in detrital thermochronology is determination of lag time, defined as the difference between the cooling age and depositional age for a detrital mineral (Garver et al. 1999). Detrital minerals can be recycled through multiple erosional and depositional cycles (Sherlock 2001, Reiners et al. 2005a). Even so, there is good evidence that in active orogens, the time between erosion and deposition is likely very short (<1 Myr) when compared to the amount of time associated with exhumation (Copeland & Harrison 1990, Heller et al. 1992, Bernet et al. 2004, Stewart & Brandon 2004). If cooling occurred by erosion, then the lag time can be used to estimate erosion rates in the source region of the sediment. The relationships in Figure 4 could be used for cases where lag times were steady or changed slowly with time (quasi-steady). Evolution of lag time through a stratigraphic sequence can
then be interpreted as evolution of spatially averaged exhumation rates in the source. Decreasing lag times upsection would represent increasing exhumation rates through time, consistent with a constructional phase of mountain building, whereas increasing lag times would suggest a decaying mountain range, and an invariant lag time through the section would be consistent with exhumational steady state—an important conclusion for tectonogeomorphic studies. A potential complication to lag time interpretations of this type includes the possibility for exhumation and cooling ages produced by tectonic, rather than erosional, exhumation. Shallow magmatism and volcanism will also complicate the situation. In this case, the lag time is no longer related to the rate of exhumation. The success of detrital thermochronology studies in the Alps and the Himalaya has been because these areas have seen little shallow magmatism or volcanism throughout the Cenozoic.

Lag times can be interpreted from detrital cooling age distributions in several ways, depending on their form. Detrital samples commonly contain a diverse mix of grain ages and statistical methods are needed to resolve components or peaks in the age distribution (Brandon 1992, 1996, 2005, as summarized in Ehlers et al. 2005). Bernet et al. (2001) used this approach to resolve two main age peaks in FT ages of detrital zircons sourced from the Alps in seven samples ranging in depositional age from modern to 15 Ma. The youngest (P1) peak composed 15%–50% of the zircons in each sample, and represented a constant lag time of 8 Myr. They interpreted this to represent exhumational steady state of the Alps since at least 15 Ma, a conclusion that appears to conflict with other studies that have argued for increased erosion rates in the last 2–4 Myr owing to climate change (Molnar 2004, Cederbom et al. 2004).

Cooling Age Distributions of Detrital Minerals

More information on the erosional dynamics of a source region is contained in the distribution of cooling ages from a sample. Stock & Montgomery (1996) outlined a method for constraining paleorelief in orogenic drainages by considering the observed range of cooling ages and an estimate of the AER in the drainage. Essentially, the range of ages observed, \( a_r \), should be the product of the topographic relief \( R \), and the rate of change of age with elevation \( da/dz \). As discussed above, the inverse of \( da/dz \) can, subject to assumptions, be an estimate of erosion rate. Using this approach, Hodges and coworkers (Brewer et al. 2003, Hodges et al. 2005, Ruhl & Hodges 2005) have turned the relationship around to estimate time-averaged erosion rates in drainages with known or assumed relief. As an example, Ruhl & Hodges (2005) analyzed 111 single-grain \(^{40}\text{Ar}/^{39}\text{Ar}\) laser fusion ages of detrital muscovite from the Nyadi drainage in central Nepal, finding a 13.4-Myr age range. Dividing this by the \( \sim 6.2\text{-km} \) topographic relief in the drainage yields an estimated erosion rate of \( \sim 0.5 \text{ km Myr}^{-1} \), although the authors state that a more rigorous analytical screening of the data reduces the age range to 8.3 Myr and an estimated erosion rate of 0.75 km Myr\(^{-1}\). As stated above, this is a time-averaged erosion rate, which is essentially based on the mean age of the observed age distribution. The abundance of very young ages in the distribution indicate that exhumation rates increased significantly sometime after \( \sim 2–11 \text{ Ma} \). Significant changes in erosion rates over time can also be
tested by comparing the form of the probability density plot for the observed cooling ages with that predicted by combining the drainage’s hypsometric curve with the observed age-elevation trend, if known (Hodges et al. 2005). If significant mismatches occur, alternative synthetic age probability density functions with spatially varying uplift/sediment-source functions or temporally varying erosion rates could be fit to the observed one to infer detailed variations in erosion rates in space and time. For example, if a single AER could be demonstrated or assumed for a source region, differences between the observed age probability density plot and that predicted for a spatially constant erosion rate could constrain the spatial distribution of erosion and, potentially, the changing relief of the source region. Alternatively, if the spatial distribution of erosion could be demonstrated or assumed to be constant in a source region, the hypsometry and the age probability density functions could be combined to yield a synthetic AER for the region that shows changes in erosion rate with time.

Interdrainage variations in cooling age distributions of detrital minerals have also been used to elucidate first-order tectonic features of active mountain ranges. Bedrock sampling or observations in many regions is impossible due to extreme relief or dense vegetation. In such cases, detrital ages may provide the only means to map geologic structures and their controls on erosion rates. Wobus et al. (2003) observed a shift from Paleozoic-Mesoproterozoic to Miocene and younger muscovite 40Ar/39Ar cooling ages across a physiographic transition in the Himalayan foothills where no structures were previously mapped. The transition also marks a dramatic shift in cosmogenic nuclide concentrations in fluvial sediment, supporting the inference of a major, active, out-of-sequence fault in this location (Wobus et al. 2005). The coincidence of a major change in precipitation also at this location led these authors to suggest a possible positive feedback between precipitation, erosion, and rock uplift here.

**SPATIAL PATTERNS OF COOLING AGES IN OROGENS**

Whereas bedrock vertical transects of cooling ages constrain temporal changes in exhumation rates, sampling over broad areas in an orogen constrains spatial patterns of time-averaged exhumation rates. This can be useful for finding active or formerly active structures, or for elucidating the larger-scale kinematics of the orogenic system.

As described above, several studies have used spatial patterns of thermochronometric ages to identify previously unknown faults or to demonstrate large differences in uplift and exhumation rates across previously known faults. As another example, Spotila et al. (2001) used apatite (U-Th)/He dating across strands of the San Andreas Fault Zone in southern California to show that a narrow crustal sliver in this transpressional zone had experienced ~3–6 km of exhumation since 1.8 Ma.

Other studies have focused on constraining the timing and rates of slip along normal faults, using the fact that footwalls are progressively tectonically exhumed perpendicular to fault strike. Many studies have focused specifically on these issues in the classic core complexes in the Basin and Range of the western United States (Foster et al. 1991, 1993; John & Foster 1993; Howard & Foster 1996; Scott et al. 1998; Foster & John 1999; Brady 2002; Carter et al. 2004). These studies find generally consistent slip rates of ~2–7 mm/year. Estimating fault slip rates, however, can be complicated...
by the combined effects of fault geometry, advection of isotherms in the footwall, and syn- or postfaulting erosion and rotation of the footwall (Ketcham 1996, Ring et al. 1999a, Ehlers et al. 2001, Grasemann & Dunkl 2003).

**Convergent Orogens**

Spatial patterns of thermochronometric ages in convergent orogens are typically interpreted differently than in extensional settings. In some cases, cooling age variations can be related to individual structures and related to the kinematics of discrete faults or folds. At some scales, however, low-T thermochronometers are more usefully interpreted in the context of overall movement of material through an orogenic system. In this context, a few large structures, such as orogen-bounding thrust faults, may set the boundary conditions for deformation within the orogen, but individual structures are ephemeral, and the particle paths of materials moving through an orogen can appear continuous at the scale of the orogen.

This perspective has been aided by the critical wedge model. Critical wedge theory was originally developed to describe the growth, form, and deformation within submarine accretionary complexes or thin-skinned fold-and-thrust belts, where crustal thickening is caused by horizontal accretion of rock directly above a subducting plate (Chapple 1978; Davis et al. 1983; Dahlen 1984, 1990). The essential principles and processes governing critical wedge behavior have since been generalized to a wide range of orogens. The fundamental feature of the theory is that the overall form of the orogen and the deformation within it are governed by the interaction of gravitational forces set by the topographic form of the wedge, the basal shear stress on the decollement beneath it, and the fact that every point within the deforming wedge is at the point of plastic failure. The criticality of a critical wedge arises from the self-adjustment of surface slopes to critical angles so that gravitational forces maintain every point in the interior of the wedge at plastic failure.

Patterns of cooling ages within orogenic wedges provide a useful way to characterize tectonic features, such as the distribution and magnitude of accretionary and erosional fluxes. One of the best-studied orogenic wedges is the emergent part of the Cascadia subduction zone—the Olympic Mountains, in western Washington State (Figure 7). Brandon et al. (1998) reported AFT ages across the Olympics wedge, and used an erosion-rate dependent crustal thermal model to invert

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**Figure 7**

Wedgeology of the Olympic Mountains, Washington State. Upper panel: Digital elevation model of the Olympic Mountains and Cascadia region, showing location of A-A’ transect shown in bottom panel. Middle panel: Schematic cross-section from west to east through the range, illustrating the geodynamic setting and presumed particle paths through the wedge (after Batt et al. 2001). Lower panel: Erosion rates inferred from strath terraces (*red and light blue symbols*) and AFT ages (*yellow symbols*), the latter using the methods summarized in this review (after Brandon et al. 1998). Precipitation (*blue line*) is the mean annual rate for 30 years, from Spatial Climate Analysis Service, Oregon State University ([http://www.ocs.oregonstate.edu/prism/](http://www.ocs.oregonstate.edu/prism/)).
these ages for time-averaged erosion rates. The results (Figure 7) show a maximum erosion rate of about 1 km Myr$^{-1}$ on the windward side of the range, which decreases to zero across the range, in the direction of plate convergence. These erosion rates, as well as their spatial variation, which represent estimates averaged over timescales of about 7 to 15 Myr, are remarkably consistent with fluvial incision rates determined from abandoned river channels, about 65 and 140 ka in age, that are now preserved as uplifted remnants above the modern river channel (Pazzaglia & Brandon 2001). This result indicates that erosion rates at the regional scale are similar to river incision rates at the local scale. This observation, and others, indicate that the erosion and uplift are in balance and that the long-wavelength topography of the Olympics has been steady since $\sim$15 Ma (Brandon et al. 1998, Pazzaglia & Brandon 2001, Batt et al. 2001).

Further study of the Olympic wedge by Batt et al. (2001) showed that bedrock ages of the ZFT, AFT, and AHe systems, with their strongly contrasting thermal sensitivities, showed nested concentric resetting zones. Using a two-dimensional kinematic and thermal model of the range as a steady-state wedge, they used the spatial pattern of ages for each system to model two-dimensional particle paths within the wedge, subject to two free parameters and constrained by best-fit results to all three thermochronometric systems. The first free parameter represented the relative flux of material into the wedge, whether by frontal accretion at the toe of the wedge or by underplating deep beneath it. The second free parameter was the maximum erosion rate at the surface of the wedge. The erosion rate profile was assumed to have the form shown in the lower panel of Figure 7, but the intensity of the erosion was allowed to vary according to the maximum erosion rate parameter. The steady-state requirement indicated that local rates for rock uplift and erosion were equal. The best-fit solutions demonstrated that accretion occurs primarily at the front of the wedge and the maximum erosion rate parameter is 0.9–1.0 km Myr$^{-1}$, Frontal accretion results in a significant gradient in horizontal velocities across the Olympics, equal to a decrease of about 3 mm year$^{-1}$ toward the northwest along the A-A’ profile in Figure 7 (Pazzagalia & Brandon 2001).

Horizontal transport explains why regions of many wedges show thermochronologic evidence for high exhumation rates for long periods of time, but expose only weakly metamorphosed rocks. In other words, the vertical component of exhumation for many rocks in these settings comprises only a minor part of the total path through the wedge. This is important because it means that the thermal history experienced by rocks in the orogen may be strongly influenced by paths where the horizontal transport is much greater than the vertical transport (Batt & Brandon 2002). Rocks that never exceeded PRZ temperatures of a given thermochronologic system during residence in the orogen may have young ages after exhumation. These ages may appear reset, but the effective closure temperature concept would not apply since the samples did not pass entirely through the PRZ.

**Climate-Tectonic Feedbacks**

The critical wedge model has important implications for the relationships between erosion, tectonics, and climate. An important feature of critical wedge theory is that...
the links between gravitational forces, shear stress, and internal plastic failure set the
form of a convergent wedge so that the cross-section of the wedge will grow in a
self-similar fashion. The balance between erosional and accretionary fluxes deter-
mine whether the wedge will grow, shrink, or remain constant in size. Importantly,
this means that the wedge must deform internally to match accretionary fluxes with
erosional fluxes while maintaining its critical taper form.

Erosion rates may be localized within an orogen by focused fluvial erosion, which
has been proposed as a mechanism for strong localization of deformation and rock
2004). On a broader scale, variations in precipitation are likely to cause variations in
erosion rates, which suggests a potentially important feedback between climate and
tectonic stresses at the orogen scale (Willett 1999). This erosional feedback, as well as other
fundamental features of the critical wedge model, are expected to hold for a much
wider range of convergent orogenic settings and scales than the submarine accre-
tionary complexes or fold-and-thrust belts for which they were originally developed
Beaumont 1994, Royden 1996, Koons et al. 2003). In other words, a generalized
concept of critical topography can probably be applied to most if not all convergent
orogens (Willett 1999).

Thermochronologic evidence for correlations between modern precipitation and
and long-term erosion rates within orogens has been presented for several orogens, in-
cluding Irian Jaya, Indonesia (Weiland & Cloos 1996), the Olympic Peninsula (Willett
1999), the central Washington Cascades (Reiners et al. 2003a), and the Himalayan
front (Wobus et al. 2003). Common to all these examples is a pronounced offset of the
maximum height of the topography with those for the erosion rate and precipitation.
In all cases, faster erosion and greater precipitation are found on the windward side
of the orogen. In the Himalayan case, Wobus et al. (2005) inferred that an individual
out-of-sequence thrust is responsible for a sharp change in erosion rate over a short
distance, but in other cases, the activity of individual structures is not apparent.

The Cascades transect shows a relatively smooth gradient in exhumation rates (as
inferred from AHe ages) across the range, although rates are relatively scattered in the
region with the highest values (Figure 8). The scatter may result from transients in
topography, geothermal gradients, or the erosion rates themselves. In this part of
the orogen, the Cascades comprise dominantly uplifted crystalline basement. Although
one might worry that transient magmatic cooling may have affected some of the
cooling ages, we note that nearly all apatite He ages are significantly younger than
intrusion ages, and so likely reflect erosional exhumation.

The unusual uplifted arc setting of the central and northern Cascades make it
difficult to interpret the kinematic origin or dynamic significance of the cross-range
AHe age pattern, and its apparent coupling with modern precipitation rate, at least in
terms of a classical critical wedge model. The lack of sharp breaks in the pattern is not
easily reconcilable with uplift by slip on discrete faults. Seismicity shows no evidence
of active discrete structures in the Cascade Range. Nevertheless, close correspondence
between the patterns of precipitation and erosion rate is striking. One specu-
lative possibility for this correlation is that uplift and exhumation in the Washington
Cascades may be due to coupling between erosion and magmatic intrusions at depth, fed by the active arc. Although there is no dynamic model for arc-related orogens analogous to the critical wedge model, it is possible that strain and exhumation in such a setting may occur by mobilization of melt-weakened crust or plutons, rather than by faults, so that weakened crust or magmas are preferentially emplaced beneath regions of high erosional exhumation. This may be similar to the models of lateral extrusion of melt-weakened crust owing to high precipitation at the edge of the Tibetan plateau (Beaumont et al. 1992, 2001; Hodges et al. 2004), and the model of channelized flow and crustal aneurysm due to focused fluvial erosion at the syntaxes of the Himalaya (Zeitler et al. 2001, Koons 2002).

Glacial Erosion

The rugged high-relief topography characteristic of many modern mountain ranges owes much of its development to Quaternary glacial erosion. Dramatic topographic features provide clear qualitative evidence of the erosive potential of glaciers (e.g., Montgomery 2002), and measurements of sediment fluxes from glacially eroded catchments have been used to argue that glacial erosion rates are one to two orders of magnitude higher than fluvial erosion rates (Hallet et al. 1996). In addition to increasing topographic relief by valley deepening, some studies have suggested that glaciers may also increase peak heights, via isostatically induced uplift (Molnar & England 1990, Small & Anderson 1998), although this remains controversial (Whipple et al. 1999, Tomkin & Braun 2002). On both global and regional scales, the remarkable correspondence between regional peak heights and equilibrium-line altitudes (ELAs) of glaciers suggests that glaciers may also act as buzz saws that limit maximum elevations (Porter 1981, Broecker & Denton 1990, Brozovic et al. 1997).

If the rapid pace of glacial erosion suggested by short-term sediment yields persist over million-year timescales, and if glaciers do act as regionally important topographic buzz saws, they should produce clear thermochronologic signals in bedrock or detrital cooling-age patterns. Thermochronologic assessments of the general importance of glacial erosion thus far, however, show mixed results. Using He dating, Spotila et al.

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**Figure 8**

Top panel: Mean elevation of topography in a 50-km wide east-west swath through the Washington Cascades at about the latitude of Seattle (green line), with apatite (U-Th)/He ages of samples within the swath. AHe ages are mean ages of two to six single-grain analyses per sample (only one point per sample is shown); 6% (2 RSE) error bars represent typical reproducibility among replicate analyses. AHe ages show an overall U-shaped pattern with distance, varying from approximately 4.0 to 60 Ma across the range, with a minimum about halfway up the west flank of the range. This figure shows new data not shown in a similar figure in Reiners et al. (2003a). Bottom panel: Erosion rates estimated for each sample using the steady-state method illustrated in Figure 4. Also shown is the mean annual precipitation rate over a ~30-year period (Spatial Climate Analysis Service, Oregon State University, http://www.ocs.oregonstate.edu/prism/). Both precipitation and erosion show an order of magnitude variation, with maxima that are displaced towards the windward side of the range.
(2004) showed that long-term (10^6 years) erosion rates in the Chugach Mountains are well correlated with the distribution of modern glaciers. Furthermore, accretionary and erosional fluxes appear to be in balance at the scale of orogen, but these rates are no greater than ~3 mm/year, which is an order of magnitude lower than short-term measurements of glacial erosion (Hallet et al. 1996). T.A. Ehlers, K.A. Farley, M.E. Rusmore & G.J. Woodsworth (manuscript submitted) also found long-term (<1–10 Myr) rates of less than 1 mm/year in the highly glaciated landscape of the Coast Mountains of British Columbia. However, Ehlers et al. (manuscript submitted) also used regional patterns of AHe ages to suggest that topographic relief has increased by 1.6–2.2 km and valleys have widened dramatically since 7.5 Ma. Using ^4He/He thermochronometry on some of the same samples, Shuster et al. (2005) concluded that at least 2 km of valley incision occurred, beginning at 1.8 ± 0.2 Ma, requiring local erosion rates over this duration of at least 5 km Myr^−1. Although this rate is far lower than short-term sediment yield estimates of Hallet et al. (1996), these results suggest that, at least locally, glacial erosion rates can be much higher than regional erosion rates. However, when measured as valley-bottom incision rates, fluvial erosion rates can also be quite high (e.g., Burbank et al. 1996, Lave & Avouac 2001). This points out the difficulty in assigning the importance of one erosional mechanism over another when erosion rates can vary by orders of magnitude over different spatial and temporal scales in a single orogen.

A more general question of the significance of glacial erosion is how it might affect the tectonic behavior of mountain ranges. As described above, numerous studies have highlighted the important role erosion may play in limiting the elevation and width of orogens, in the context of a critical wedge (Dahlen & Barr 1989, Willett 1999, Hilley & Strecker 2004, Whipple & Meade 2004). If glaciation can indeed act as a topographic buzz saw, then the onset of glacial conditions and lowering of the ELA should rapidly decrease the elevation of an orogen. This erosion will induce a rock uplift response, but the magnitude and distribution of the response will depend on the tectonic conditions of the range. If the range is tectonically inactive, uplift will be limited to isostatic rebound, and the change in erosion rate for areas intersecting the ELA will be inversely proportional to the isostatic compensation ratio (~0.2; Pazzaglia & Brandon 1996), flexural effects notwithstanding. If the range behaves as a critical orogenic wedge (see Sidebar), however, the consequences are more interesting. The descending ELA will intersect and rapidly erode the crest of the wedge, decreasing its elevation. Maintenance of critical taper dictates that the wedge will respond not only by increasing uplift rates in this portion of the wedge, but also by decreasing the overall wedge width, which requires even faster erosion. Numerical simulations of both passive and active wedge scenarios for typical wedge parameters, using ELA lowering rates estimated for Quaternary glacial cycles (Broecker & Denton 1990), predict changes in erosion rates of about 0.5 to 2 km Myr^−1 (J.H. Tomkin & M.T. Brandon, manuscript submitted), which should be easily detectable using standard He or FT dating approaches. Testing for the orogenic response to alpine glaciation in such a scenario could be done by examining both timing and magnitudes of erosional rate changes along strike of ELA-lowering gradients such as latitude.
CRITICAL OROGENIC WEDGE

The critical orogenic wedge is a deforming wedge of crustal material that forms where plates converge. The wedge is bounded by a basal thrust or decollement (Figure 7) that allows one plate to subduct beneath another. Some material is transferred by accretion from the subducting plate to the overriding plate, causing the wedge to deform and grow with time. The wedge will deform internally until it reaches a critical taper in which the wedge is blunt enough and strong enough to overcome the resistance to slip on the decollement. Further accretion at the front of the wedge or erosion at the top of the wedge will reduce the taper and the integrated strength of the wedge. The wedge will respond by deforming and thicken internally until it recovers a blunter and stronger taper. This feedback causes an orogenic wedge to remain close to its critical taper when perturbed by frontal accretion and erosion. The critical wedge model predicts that spatially focused erosion should result in spatially focused deformation and rock uplift.

SUMMARY POINTS

1. Erosion denudes orogens and exhumes rocks. Spatial patterns of erosion in orogens can influence tectonic deformation and uplift. For example, focused orographic precipitation can cause focused erosion, which may lead to focused tectonic strain. Thermochronology can constrain spatial-temporal patterns of erosion in orogens on \( \sim 10^6 \)–\( 10^7 \) year timescales, commensurate with cycles of orogenic growth and decay, and the response time for possible feedbacks between climate and tectonics.

2. The most commonly used low- to intermediate-temperature thermochronometers use \((\mathrm{U}-\mathrm{Th})/\mathrm{He}\) and fission-track systems in U-Th-bearing minerals, most commonly apatite and zircon, and the \( \text{Ar}/\text{Ar} \) (and K/Ar) systems in feldspar, micas, and hornblende. Diffusion of \( \text{He} \) and \( \text{Ar} \) and annealing of fission tracks are well represented by thermally activated diffusion, which allows quantitative predictions of the thermal sensitivities of the thermochronometers. The partial retention zone (PRZ) describes the temperature range where thermochronometers are able to only partially retain the products of radioactive decay (\( \text{He} \), fission tracks, \( \text{Ar} \)). The loss-only PRZ temperatures range from \( \sim 20 ^\circ \mathrm{C} \)–\( 60 ^\circ \mathrm{C} \) for the apatite He system to \( \sim 400 ^\circ \mathrm{C} \)–\( 525 ^\circ \mathrm{C} \) for the hornblende \( \text{Ar}/\text{Ar} \) system and correspond to crustal depths of \( \sim 1 \) km to several tens of kilometers.

3. For monotonic cooling histories, the thermal sensitivity of each system can be represented by an effective closure temperature, which is the temperature of the mineral at the measured thermochronometric age (the cooling age).
for steady monotonic cooling. Closure temperatures for commonly used thermochronometers range from about 65°C to 550°C for the apatite He and hornblende Ar systems, respectively, assuming typical orogenic cooling rates.

4. Given a crustal thermal model, which can be adapted to specific orogenic settings, thermochronometric cooling ages can be uniquely related to an erosion rate, assuming this rate has been steady prior to and after closure of the system. Changes in erosion rate can cause transient movement of isotherms relative to Earth’s surface, which can invalidate this estimate. Thermochronometers with low closure temperatures are able to recover more rapidly from transients and thus are more likely to follow the steady-state solution.

5. Changes in erosion rates with time can be constrained from measurements of multiple cooling ages from the same rock, provided transient thermal effects are considered, or from the distribution of cooling ages of a single system with elevation in vertical transects. Age-elevation relationships in a vertical transect can provide two estimates of erosion rates. The first estimate is given by the slope of the age-elevation profile and is representative of the time interval represented by the cooling ages. The second estimate is representative of the average erosion rate over the time interval from the cooling age at the mean elevation of the profile to present. Key assumptions for the vertical transect method are that the closure isotherm is relatively flat under the study area and remained at a constant depth during the time interval represented by the cooling ages in the profile.

6. Detrital thermochronology uses the distribution of grain ages from a single sample of sediment or sedimentary rock to constrain the exhumational history of the source region of the sediment. Lag time represents the amount of time that elapsed between passage of the dated grain through the closure depth for the thermochronometer and deposition of the sediment. Changes in lag times in sediments shed from the same orogen over time can constrain the growth and decay of the orogen. Detrital grain age distributions can also be used to constrain paleorelief, and determine spatial or temporal variations in exhumation rates.

7. Spatial patterns of bedrock cooling ages in orogens can be used to map out variations in erosion rates and their relationships with kinematic models for material flow through orogenic wedges, climatic variations, or structural or geomorphic features. In some cases, spatial patterns of thermochronometrically determined erosion rates are strikingly similar to those determined from much shorter-term geomorphic features, or to modern patterns of precipitation.
FUTURE DIRECTIONS

1. Many of the recent advances in the methods, interpretations, and applications of thermochronology have been motivated by growing interest in the connections between tectonic, geomorphic, and climatic processes. Partly as a result, considerable interest has focused on thermochronometers sensitive to low temperatures, such as apatite FT and He. One emerging method with great potential to extend the sensitivity to even lower temperatures, as well as estimate continuous time-temperature paths during exhumation, is $^4\text{He}/^3\text{He}$ thermochronometry (Shuster et al. 2003, 2005; Shuster & Farley 2003, 2005). This method measures intracrystalline $^4\text{He}$ distributions to resolve the cooling path from $\sim 80^\circ \text{C}$ to the surface. Intracrystalline $^4\text{He}$ variations may also be measured in other ways (such as in situ laser ablation), opening up the possibility of routinely estimating cooling paths rather than a single closure temperature.

2. As is well-known from detrital studies, many problems in orogenic systems require thermochronologic data from large areas involving many samples and individual grain ages. This approach allows one to image broad-scale tectonic or erosional patterns and simply reduce statistical uncertainty. A challenge for thermochronology is to find ways to increase the number of grains that can be dated while maintaining good precision. The availability of synoptic datasets for large areas or distributions of hundreds of detrital grain ages from single catchments will lead to new discoveries in how surface processes affect the orogenic systems.

3. There is growing interest in combining thermochronology with other approaches to study orogenic evolution. Examples include using combined thermochronologic and cosmogenic methods with river chemistry and climate data to understand the interrelation between physical and chemical erosion at different timescales.

4. In general, there is a need for a more robust understanding of the interaction of tectonics, erosion, and climate in orogenic systems. Although theoretical approaches suggest important linkages between them, actual evidence from thermochronologic or other approaches is often ambiguous. Important progress will come from well-posed natural experiments that will allow a close examination of climate, surface processes, and tectonics at different time- and length-scales.

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Errata for:


1) The number 1 is missing from the denominator with the exponential expression in equation 8a. The correct equation is:

\[
T(z) = T_S + \left( T_L - T_S + \frac{H_T L}{\dot{\epsilon}} \right) \frac{1 - \exp\left(-\frac{\dot{\epsilon}}{\kappa} z\right)}{1 - \exp\left(-\frac{\dot{\epsilon}}{\kappa} L\right)} - \frac{H_T z}{\dot{\epsilon}},
\]  

(8a)

2) The temperatures for the PRZ temperatures for the He and Ar systems shown in Figures 1a and 1c were incorrectly calculated due to a numerical error in the CLOSURE program. The temperatures were systematically too low by about 25°C. Corrected versions of these figures are included here. A corrected version of the CLOSURE program is available at www.geology.yale.edu/~brandon.

Note that these errors do not change any of the discussion or conclusions of our paper.
Reiners and Brandon (2006)
Figure 1a. Loss-only PRZ for He dating calculated using CLOSURE (corrected, June 24, 2007)
Reiners and Brandon (2006)
Figure 1b. Loss-only PRZ for FT dating calculated using CLOSURE (original published version was correct; included here for completeness).
Reiners and Brandon (2006)
Figure 1c. Loss-only PRZ for Ar dating calculated using CLOSURE (corrected, June 24, 2007)